### **Compare Fractions Using Benchmarks**

**Essential Question** How can you use benchmarks to compare fractions?

# Unlock the Problem

David made a popcorn snack. He mixed  $\frac{5}{8}$  gallon of popcorn with  $\frac{1}{2}$  gallon of dried apple rings. Did he use more dried apple rings or more popcorn?



**Materials fraction** strips

Use fraction strips to compare  $\frac{5}{8}$  and  $\frac{1}{2}$ . Record on the model below.

1/2	1/2				1/2			
<u>5</u> 8	1/8	18	<u>1</u> 8	<u>1</u>	<u>1</u> 8	18	<u>1</u> 8	<u>1</u> 8



So, David used more \_\_\_\_

- **1.** Write five fractions equivalent to  $\frac{1}{2}$ . What is the relationship between the numerator and the denominator of fractions equivalent to  $\frac{1}{2}$ ?
- **2.** How many eighths are equivalent to  $\frac{1}{2}$ ?
- **3.** How can you compare  $\frac{5}{8}$  and  $\frac{1}{2}$  without using a model?

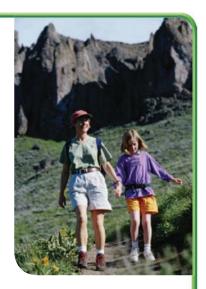


**Look for Structure How** are the number of eighthsize parts in  $\frac{5}{8}$  related to the number of eighth-size parts you need to make  $\frac{1}{2}$ ? **Benchmarks** A benchmark is a known size or amount that helps you understand a different size or amount. You can use  $\frac{1}{2}$  as a benchmark to help you compare fractions.

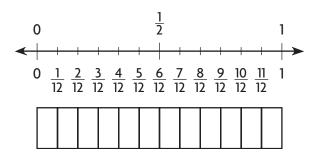


A family hiked the same mountain trail. Evie and her father hiked  $\frac{5}{12}$  of the trail before they stopped for lunch. Jill and her mother hiked  $\frac{9}{10}$  of the trail before they stopped for lunch. Who hiked farther before lunch?

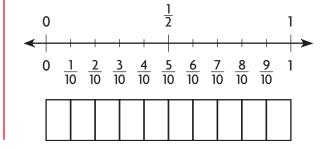
Compare  $\frac{5}{12}$  and  $\frac{9}{10}$  to the benchmark  $\frac{1}{2}$ .



**STEP 1** Compare  $\frac{5}{12}$  to  $\frac{1}{2}$ .



**STEP 2** Compare  $\frac{9}{10}$  to  $\frac{1}{2}$ .



Think: Shade  $\frac{5}{12}$ .

 $\frac{5}{12} \bigcirc \frac{1}{2}$ 

Think: Shade  $\frac{9}{10}$ .

 $\frac{9}{10} \bigcirc \frac{1}{2}$ 

Since  $\frac{5}{12}$  is \_\_\_\_\_ than  $\frac{1}{2}$  and  $\frac{9}{10}$  is \_\_\_\_ than  $\frac{1}{2}$ , you know that  $\frac{5}{12}$   $\bigcirc$   $\frac{9}{10}$ .

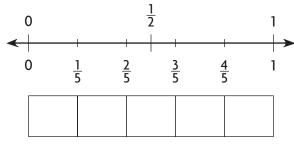
So, \_\_\_\_\_\_hiked farther before lunch.

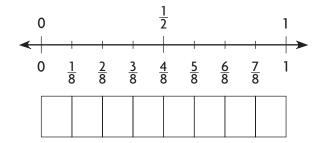
- **4.** Explain how you can tell  $\frac{5}{12}$  is less than  $\frac{1}{2}$  without using a model.
- **5.** Explain how you can tell  $\frac{7}{10}$  is greater than  $\frac{1}{2}$  without using a model.

## **Share and Show**



**1.** Compare  $\frac{2}{5}$  and  $\frac{1}{8}$ . Write < or >.





$$\frac{2}{5}$$
  $\frac{1}{8}$ 

Compare. Write < or >.

- **② 2.**  $\frac{1}{2}$   $\frac{4}{6}$
- 3.  $\frac{3}{10}$   $\frac{1}{2}$
- **4.**  $\frac{11}{12}$   $\frac{4}{8}$
- 5.  $\frac{5}{8}$   $\frac{2}{5}$

## Math Talk

#### MATHEMATICAL PRACTICES 6

Compare How do you know  $\frac{1}{3} < \frac{1}{2}$ ?

#### On Your Own

Compare. Write < or >.

- **6.**  $\frac{8}{10}$   $\frac{3}{8}$
- 7.  $\frac{1}{3}$   $\frac{7}{12}$
- 8.  $\frac{2}{6}$
- **9.**  $\frac{4}{8}$   $\frac{2}{10}$

MATHEMATICAL 2 Reason Quantitatively Algebra Find a numerator that makes the statement true.

- 11.  $\frac{8}{10} > \frac{1}{8}$
- **12.**  $\frac{10}{12} > \frac{10}{4}$
- 13.  $\frac{2}{5} < \frac{10}{10}$
- **14.** When two fractions are between 0 and  $\frac{1}{2}$ , how do you know which fraction is greater? Explain.
- **15.** Godesper If you know that  $\frac{2}{6} < \frac{1}{2}$  and  $\frac{3}{4} > \frac{1}{2}$ , what do you know about  $\frac{2}{6}$  and  $\frac{3}{4}$ ?
- **16.** Godesper Sandra has ribbons that are  $\frac{3}{4}$  yard,  $\frac{2}{6}$  yard,  $\frac{1}{5}$  yard, and  $\frac{4}{7}$  yard long. She needs to use the ribbon longer than  $\frac{2}{3}$  yard to make a bow. Which length of ribbon could she use for the bow?



## **Problem Solving • Applications**

**17.** HINKSMARTER Saundra ran  $\frac{7}{12}$  of a mile. Lamar ran  $\frac{3}{4}$  of a mile. Who ran farther? Explain.



**WRITE** Math • Show Your Work

- **18. What's the Question?** Selena ran farther than Manny.
- **19.** Chloe made a small pan of ziti and a small pan of lasagna. She cut the ziti into 8 equal parts and the lasagna into 9 equal parts. Her family ate  $\frac{2}{3}$  of the lasagna. If her family ate more lasagna than ziti, what fraction of the ziti could have been eaten?
- **20.** ITHINKSMARTER James, Ella, and Ryan biked around Eagle Lake. James biked  $\frac{2}{10}$  of the distance in an hour. Ella biked  $\frac{4}{8}$  of the distance in an hour. Ryan biked  $\frac{2}{5}$  of the distance in an hour. Compare the distances biked by each person by matching the statements to the correct symbol. Each symbol may be used more than once or not at all.





$$\frac{4}{9}$$
  $\frac{2}{5}$ 



$$\frac{2}{10}$$
  $\frac{2}{5}$  •

•>

## **Compare Fractions Using Benchmarks**

Compare. Write < or > .

1.  $\frac{1}{8}$  <  $\frac{6}{10}$ 

**2.**  $\frac{4}{12}$   $\frac{4}{6}$ 

3.  $\frac{2}{8}$   $\frac{1}{2}$ 

Think:  $\frac{1}{8}$  is less than  $\frac{1}{2}$ .

 $\frac{6}{10}$  is more than  $\frac{1}{2}$ .

**4.**  $\frac{3}{5}$   $\frac{3}{3}$ 

5.  $\frac{7}{8}$   $\frac{5}{10}$ 

**6.**  $\frac{9}{12}$ 

**7.**  $\frac{4}{6}$   $\frac{7}{8}$ 

**8.**  $\frac{2}{4}$   $\frac{2}{3}$ 

**9.**  $\frac{3}{5}$   $\frac{1}{4}$ 

**10.**  $\frac{6}{10}$   $\frac{2}{5}$ 

**11.**  $\frac{1}{8}$   $\frac{2}{10}$ 

**12.**  $\frac{2}{3}$   $\frac{5}{12}$ 

## **Problem Solving**



- **13.** Erika ran  $\frac{3}{8}$  mile. Maria ran  $\frac{3}{4}$  mile. Who ran farther?
- **14.** Carlos finished  $\frac{1}{3}$  of his art project on Monday. Tyler finished  $\frac{1}{2}$  of his art project on Monday. Who finished more of his art project on Monday?

**15.** WRITE Math Explain a strategy you could use to compare  $\frac{2}{6}$  and  $\frac{5}{8}$ .

#### **Lesson Check** (4.NF.A.2)

**1.** What symbol makes the statement true?

**2.** Write a fraction, less than 1, with a demoninator of 6 that is greater than  $\frac{3}{4}$ .



#### **Spiral Review** (4.0A.A.3, 4.0A.B.4, 4.NBT.B.6)

- 3. Abigail is putting tiles on a table top. She needs 48 tiles for each of 8 rows. Each row will have 6 white tiles. The rest of the tiles will be purple. How many purple tiles will she need?
- **4.** Each school bus going on the field trip holds 36 students and 4 adults. There are 6 filled buses on the field trip. How many people are going on the field trip?

- 5. Noah wants to display his 72 collector's flags. He is going to put 6 flags in each row. How many rows of flags will he have in his display?
- **6.** Julian wrote this number pattern on the board:

3, 10, 17, 24, 31, 38. Which of the numbers in Julian's pattern are composite numbers?