## Common Denominators

## Unlock the Problem

Martin has two rectangles that are the same size. One rectangle is cut into $\frac{1}{2}$-size parts. The other rectangle is cut into $\frac{1}{3}$-size parts. He wants to cut the rectangles so they have the same size parts. How can he cut each rectangle?

A common denominator is a common multiple of the denominators of two or more fractions. Fractions with common denominators represent wholes cut into the
 same number of parts.

## (1) Activity use paper folding and shading.

Materials $\quad 2$ sheets of paper
Find a common denominator for $\frac{1}{2}$ and $\frac{1}{3}$.

## STEP 1

Model the rectangle cut into $\frac{1}{2}$-size parts. Fold one sheet of paper in half. Draw a line on the fold.

## STEP 2

Model the rectangle cut into $\frac{1}{3}$-size parts. Fold the other sheet of paper into thirds. Draw lines on the folds.

## STEP 3

Fold each sheet of paper so that both sheets have the same number of parts. Draw lines on the folds. How many equal
parts does each sheet of paper have? $\qquad$

Use Models How did the models help you find the common denominator for $\frac{1}{2}$ and $\frac{1}{3}$ ?

## STEP 4

Draw a picture of your sheets of paper to
show how many parts each rectangle could have.

So, each rectangle could be cut into $\qquad$ parts.

## Example write $\frac{4}{5}$ and $\frac{1}{2}$ as a pair of fractions with common denominators.

You can use common multiples to find a common denominator. List multiples of each denominator. A common multiple can be used as a common denominator.

STEP 1 List multiples of 5 and 2.
Circle common multiples.

5: 5 ,

2 : $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$

STEP 2 Write equivalent fractions.
$\frac{4}{5}=\frac{4 x}{5 x}=\frac{}{10}$
$\frac{1}{2}=\frac{1 x}{2 x}=\frac{}{10}$
Choose a denominator that is a common multiple of 5 and 2 .

You can write $\frac{4}{5}$ and $\frac{1}{2}$ as $\qquad$ and $\qquad$ -

1. Are $\frac{4}{5}$ and $\frac{1}{2}$ equivalent? Explain.
$\qquad$
$\qquad$ fraction.

## ERROR Alert

Remember that when you multiply the denominator by a factor, you must multiply the numerator by the same factor to write an equivalent
2. Describe another way you could tell whether $\frac{4}{5}$ and $\frac{1}{2}$ are equivalent.
$\qquad$
$\qquad$
$\qquad$

## Shape and Show

## MATH <br> BOARD

1. Find a common denominator for $\frac{1}{3}$ and $\frac{1}{12}$ by dividing each whole into the same number of equal parts.
Use the models to help.
common denominator: $\qquad$

$\frac{1}{3}$

$\frac{1}{12}$

Name
Write the pair of fractions as a pair of fractions with a common denominator.
2. $\frac{1}{2}$ and $\frac{1}{4}$
3. $\frac{3}{4}$ and $\frac{5}{8}$
4. $\frac{1}{3}$ and $\frac{1}{4}$
5. $\frac{4}{12}$ and $\frac{5}{8}$

## On Your Own

Explain how using a model or listing multiples helps you find a common denominator.

Write the pair of fractions as a pair of fractions with a common denominator.
6. $\frac{1}{4}$ and $\frac{5}{6}$

Tell whether the fractions are equivalent. Write $=$ or $\neq$.
8.

9. $\frac{3}{4} \bigcirc \frac{6}{8}$
10. $\frac{1}{2} \bigcirc \frac{4}{8}$
11. $\frac{6}{8} \bigcirc \frac{4}{8}$
12. GODEEPER Jerry has two same-size circles divided into the same number of equal parts. One circle has $\frac{3}{4}$ of the parts shaded, and the other has $\frac{2}{3}$ of the parts shaded. His sister says the least number of pieces each circle could be divided into is 7 . Is his sister correct? Explain.

## Problem Solving • Applications (acald

13. GODEEPER Carrie has a red streamer that is $\frac{3}{4}$ yard long and a blue streamer that is $\frac{5}{6}$ yard long. She says the streamers are the same length. Does this make sense? Explain.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
14. THINK SMARIER Leah has two same-size rectangles divided into the same number of equal parts. One rectangle has $\frac{1}{3}$ of the parts shaded, and the other has $\frac{2}{5}$ of the parts shaded. What is the least number of parts into which both rectangles could be divided?
$\qquad$
15. 

Maritnacical (6) Julian says a common denominator for $\frac{3}{4}$ and $\frac{2}{5}$ is 9 . What is Julian's error? Explain.

## Personal Math Trainer

16. THINK SMARTER ${ }^{\text {B }}$ Miguel has two same-size rectangles divided into the same number of equal parts. One rectangle has $\frac{3}{4}$ of the parts shaded, and the other has $\frac{5}{8}$ of the parts shaded.

Into how many parts could each rectangle be divided? Show your work by sketching the rectangles.


## Common Denominators

COMMON CORE STANDARD—4.NF.A. 1
Extend understanding of fraction equivalence and ordering.
Write the pair of fractions as a pair of fractions with a common denominator.

1. $\frac{2}{3}$ and $\frac{3}{4}$
2. $\frac{1}{4}$ and $\frac{2}{3}$
3. $\frac{3}{10}$ and $\frac{1}{2}$

Think: Find a common multiple.
3: 3, 6, 9, 12, 15
4: 4, 8, 12, 16, 20
$\frac{8}{12}, \frac{9}{12}$
4. $\frac{3}{5}$ and $\frac{3}{4}$
5. $\frac{2}{4}$ and $\frac{7}{8}$
6. $\frac{2}{3}$ and $\frac{5}{12}$
7. $\frac{1}{4}$ and $\frac{1}{6}$

Tell whether the fractions are equivalent. Write $=$ or $\neq$.
8. $\frac{1}{2} \bigcirc \frac{2}{5}$
9. $\frac{1}{2} \bigcirc \frac{3}{6}$
10. $\frac{3}{4} \bigcirc \frac{5}{6}$
11. $\frac{6}{10} \bigcirc \frac{3}{5}$

## Problem Solving (red world

12. Adam drew two same size rectangles and divided them into the same number of equal parts. He shaded $\frac{1}{3}$ of one rectangle and $\frac{1}{4}$ of the other rectangle. What is the least number of parts into which both rectangles could be divided?
13. Mera painted equal sections of her bedroom wall to make a pattern. She painted $\frac{2}{5}$ of the wall white and $\frac{1}{2}$ of the wall lavender. Write an equivalent fraction for each fraction using a common denominator.

## Lesson Check (4.Nf.A.1)

1. Write a common denominator for $\frac{1}{4}$ and $\frac{5}{6}$.

## Spiral Review (4.nBT.A.2, 4.nBT.B.5, 4.NBT.B.6, 4.NF.A.1)

3. What number is 100,000 more than seven hundred two thousand, eighty-three?
4. On a bulletin board, the principal, Ms. Gomez, put 115 photos of the fourthgrade students in her school. She put the photos in 5 equal rows. How many photos did she put in each row?
5. Aiden baked 8 dozen muffins. How many total muffins did he bake?
6. Judy uses 12 tiles to make a mosaic. Eight of the tiles are blue. What fraction, in simplest form, represents the tiles that are blue?
