## **Common Denominators**

**Essential Question** How can you write a pair of fractions as fractions with a common denominator?

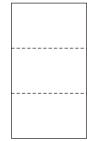
## Unlock the Problem



Martin has two rectangles that are the same size. One rectangle is cut into  $\frac{1}{2}$ -size parts. The other rectangle is cut into  $\frac{1}{3}$ -size parts. He wants to cut the rectangles so they have the same size parts. How can he cut each rectangle?

A **common denominator** is a common multiple of the denominators of two or more fractions. Fractions with common denominators represent wholes cut into the same number of parts.





Activity Use paper folding and shading.

Materials ■ 2 sheets of paper

Find a common denominator for  $\frac{1}{2}$  and  $\frac{1}{3}$ .

#### STEP 1

Model the rectangle cut into  $\frac{1}{2}$ -size parts. Fold one sheet of paper in half. Draw a line on the fold.

#### STEP 2

Model the rectangle cut into  $\frac{1}{3}$ -size parts. Fold the other sheet of paper into thirds. Draw lines on the folds.

#### STEP 3

Fold each sheet of paper so that both sheets have the same number of parts. Draw lines on the folds. How many equal

parts does each sheet of paper have?



#### MATHEMATICAL PRACTICES 4

Use Models How did the models help you find the common denominator for  $\frac{1}{2}$  and  $\frac{1}{2}$ ?

#### STEP 4

Draw a picture of your sheets of paper to show how many parts each rectangle could have.

So, each rectangle could be cut into parts.

# **Example** Write $\frac{4}{5}$ and $\frac{1}{2}$ as a pair of fractions with common denominators.

You can use common multiples to find a common denominator. List multiples of each denominator. A common multiple can be used as a common denominator.

**STEP 1** List multiples of 5 and 2. Circle common multiples.

- 5: 5,
- 10, \_\_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_
- 2: \_\_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_,

**STEP 2** Write equivalent fractions.

$$\frac{4}{5} = \frac{4 \times 1}{5 \times 1} = \frac{10}{10}$$

$$\frac{1}{2} = \frac{1 \times \dots}{2 \times \dots} = \frac{1}{10}$$

Choose a denominator that is a common multiple of 5 and 2.

You can write  $\frac{4}{5}$  and  $\frac{1}{2}$  as

and



### **ERROR Alert**

Remember that when you multiply the denominator by a factor, you must multiply the numerator by the same factor to write an equivalent fraction.

**1.** Are  $\frac{4}{5}$  and  $\frac{1}{2}$  equivalent? Explain.

**2.** Describe another way you could tell whether  $\frac{4}{5}$  and  $\frac{1}{2}$  are equivalent.

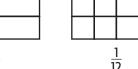
## **Share and Show**



1. Find a common denominator for  $\frac{1}{3}$  and  $\frac{1}{12}$  by dividing each whole into the same number of equal parts. Use the models to help.

common denominator:





Write the pair of fractions as a pair of fractions with a common denominator.

**2.**  $\frac{1}{2}$  and  $\frac{1}{4}$ 

3.  $\frac{3}{4}$  and  $\frac{5}{8}$ 

**4.**  $\frac{1}{3}$  and  $\frac{1}{4}$ 

**5.**  $\frac{4}{12}$  and  $\frac{5}{8}$ 

#### MATHEMATICAL PRACTICES 6

**Explain** how using a model or listing multiples helps you find a common denominator.

## On Your Own

Write the pair of fractions as a pair of fractions with a common denominator.

**6.**  $\frac{1}{4}$  and  $\frac{5}{6}$ 

7.  $\frac{3}{5}$  and  $\frac{4}{10}$ 

Tell whether the fractions are equivalent. Write = or  $\neq$ .

- **8.**  $\frac{3}{4}$   $\frac{1}{2}$
- 9.  $\frac{3}{4}$   $\frac{6}{8}$  10.  $\frac{1}{2}$   $\frac{4}{8}$
- 11.  $\frac{6}{8}$   $\frac{4}{8}$
- **12.** GODEEPER Jerry has two same-size circles divided into the same number of equal parts. One circle has  $\frac{3}{4}$  of the parts shaded, and the other has  $\frac{2}{3}$  of the parts shaded. His sister says the least number of pieces each circle could be divided into is 7. Is his sister correct? Explain.

#### Common Core

## **Problem Solving • Applications**



13. Carrie has a red streamer that is  $\frac{3}{4}$  yard long and a blue streamer that is  $\frac{5}{6}$  yard long. She says the streamers are the same length. Does this make sense? Explain.



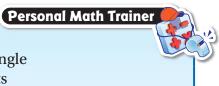
**14.** Leah has two same-size rectangles divided into the same number of equal parts. One rectangle has  $\frac{1}{3}$  of the parts shaded, and the other has  $\frac{2}{5}$  of the parts shaded. What is the least number of parts into which both rectangles could be divided?



**15.** Mathematical 3 Julian says a common denominator for  $\frac{3}{4}$  and  $\frac{2}{5}$  is 9. What is Julian's error? **Explain**.



16. THINKSMARTER + Miguel has two same-size rectangles divided into the same number of equal parts. One rectangle has  $\frac{3}{4}$  of the parts shaded, and the other has  $\frac{5}{8}$  of the parts shaded.



Into how many parts could each rectangle be divided? Show your work by sketching the rectangles.





## **Common Denominators**

Write the pair of fractions as a pair of fractions with a common denominator.

1.  $\frac{2}{3}$  and  $\frac{3}{4}$ 

2.  $\frac{1}{4}$  and  $\frac{2}{3}$ 

3.  $\frac{3}{10}$  and  $\frac{1}{2}$ 

Think: Find a common multiple.

$$\frac{8}{12}$$
,  $\frac{9}{12}$ 

**4.**  $\frac{3}{5}$  and  $\frac{3}{4}$ 

5.  $\frac{2}{4}$  and  $\frac{7}{8}$ 

- **6.**  $\frac{2}{3}$  and  $\frac{5}{12}$
- 7.  $\frac{1}{4}$  and  $\frac{1}{6}$

Tell whether the fractions are equivalent. Write = or  $\neq$ .

8.  $\frac{1}{2}$   $\frac{2}{5}$ 

9.  $\frac{1}{2}$   $\frac{3}{6}$ 

- **10.**  $\frac{3}{4}$   $\frac{5}{6}$
- **11.**  $\frac{6}{10}$   $\frac{3}{5}$

## **Problem Solving**



- **12.** Adam drew two same size rectangles and divided them into the same number of equal parts. He shaded  $\frac{1}{3}$  of one rectangle and  $\frac{1}{4}$  of the other rectangle. What is the least number of parts into which both rectangles could be divided?
- **13.** Mera painted equal sections of her bedroom wall to make a pattern. She painted  $\frac{2}{5}$  of the wall white and  $\frac{1}{2}$  of the wall lavender. Write an equivalent fraction for each fraction using a common denominator.
- **14. WRITE** Math How are a common denominator and a common multiple alike and different?

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## **Lesson Check** (4.NF.A.1)

- **1.** Write a common denominator for  $\frac{1}{4}$  and  $\frac{5}{6}$ .
- **2.** Two fractions have a common denominator of 8. What could the two fractions be?

## **Spiral Review** (4.NBT.A.2, 4.NBT.B.5, 4.NBT.B.6, 4.NF.A.1)

- **3.** What number is 100,000 more than seven hundred two thousand, eighty-three?
- **4.** Aiden baked 8 dozen muffins. How many total muffins did he bake?

- 5. On a bulletin board, the principal, Ms. Gomez, put 115 photos of the fourth-grade students in her school. She put the photos in 5 equal rows. How many photos did she put in each row?
- **6.** Judy uses 12 tiles to make a mosaic. Eight of the tiles are blue. What fraction, in simplest form, represents the tiles that are blue?

